



Tools for Teaching
Quantitative Thinking

Spotting white lies - GLM & MM

Marbella Perez Pena, Xueqing Ma, Lu Leng,
Dominik Noller, Julian Lasry



Experiment Design

- 39 participants
- 56 different video clips
- decide true or false
 - Two categories of topic, food or music
 - Actors made the video clips
 - They were asked which category they preferred before hand
 - Then actors were asked to tell truth or lie about their preference in each video clip



	▲	subj	clipn	dv	resp	clipt	clipf	clipcat	actor	ees
1		1	8	0	0	1	1	1	1	69
2		1	11	1	1	1	1	1	4	74

- clipn = Serial number of video clips
- dv = Outcome variable (correct or false guess)
- resp = Participant's guess
- clipt = Actor's statement was a truth or a lie
- clipf = Actor is talking about favorite or least favorite category
- clipcat = Category is food or music
- actor = One of seven actors
- ees = Actors' expressiveness rated by participants

Research questions

- Category: Are people more accurate at detecting lies when the category is food or music?
- Preference: Are people more accurate at detecting lies when actors are talking about their favorite category or least favorite category?
- Truthfulness: Are people more accurate at detecting lies when the statement in the clip is true?
- Expressiveness: Are people more accurate at detecting lies when the actor is more expressive?
- Actor: Are people more accurate at detecting the lies of a particular actor?

Fitting General Linear Logistic Models

```
Start:  AIC=2890.88  
dv ~ clipt + clipf + clipcat + actor + ees.c
```

```
Step:  AIC=2890.88  
dv ~ clipt + clipf + clipcat + actor
```

	Df	Deviance	AIC
- clipt	1	2871.6	2889.6
<none>		2870.9	2890.9
- clipcat	1	2882.5	2900.5
- clipf	1	2889.3	2907.3
- actor	6	2905.8	2913.8

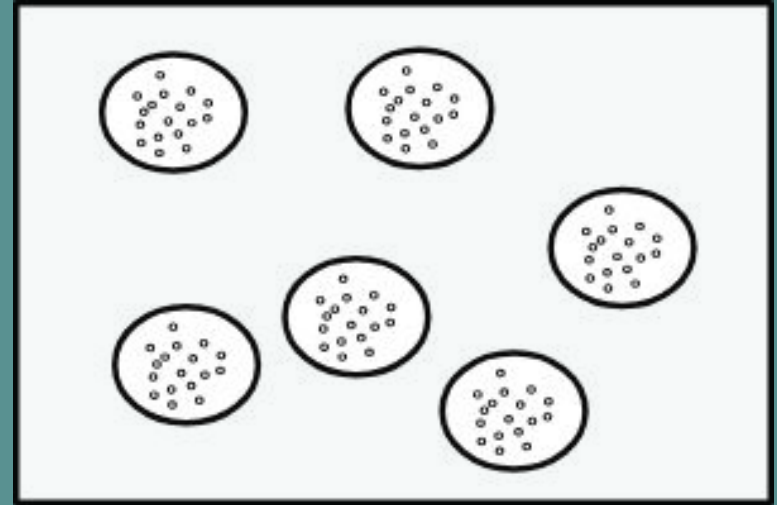
```
Step:  AIC=2889.59  
dv ~ clipf + clipcat + actor
```

	Df	Deviance	AIC
<none>		2871.6	2889.6
+ clipt	1	2870.9	2890.9
- clipcat	1	2883.2	2899.2
- clipf	1	2890.0	2906.0
- actor	6	2906.5	2912.5

- Started with generalized linear logistic models
- Considered all possible combinations of predictors using stepAIC function
- AIC measures relative statistical quality of models
- Model with lowest AIC:
dv~clipf+clipcat+actor

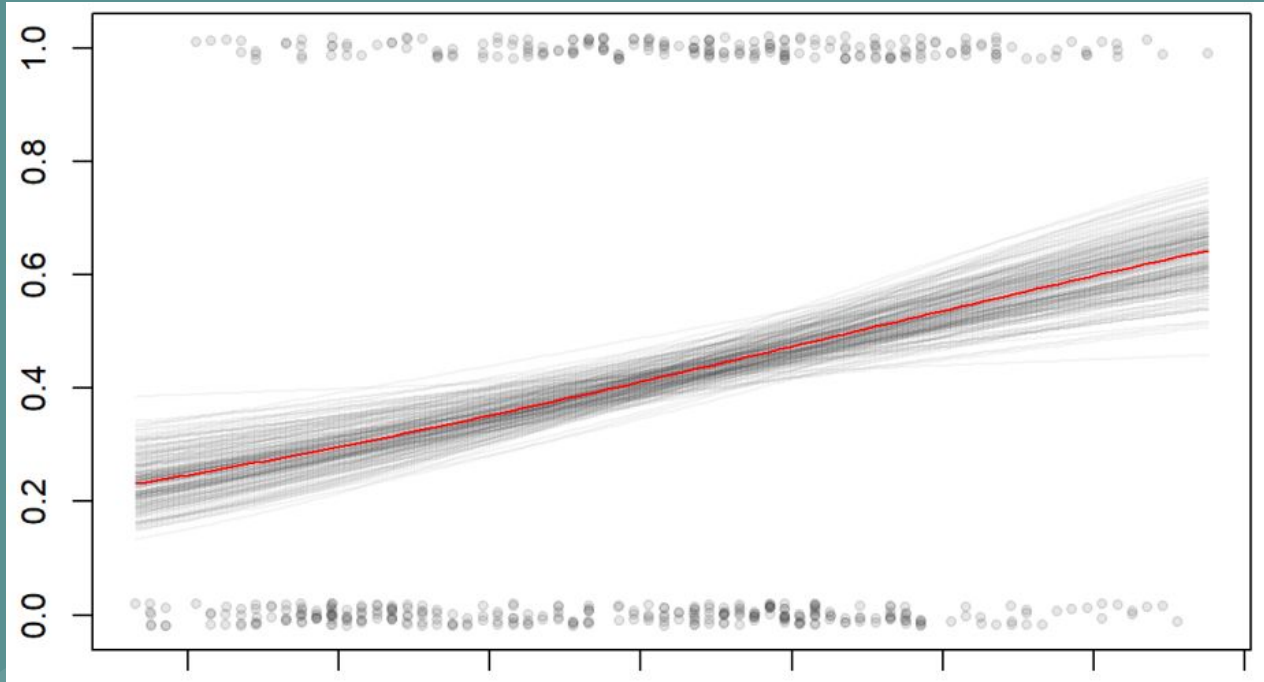
However...nested data

- Multiple measurements per subject = NOT independent
- Clips clustered by subject
- Clips grouped by actors
- Other examples:
 - Students in classrooms
 - Patients seen by same doctor
- How to deal with nested data?
 - Aggregate? No
 - Individual regressions? No
 - Mixed models? Yes!



<https://stats.idre.ucla.edu/other/mult-pkg/introduction-to-linear-mixed-models/>

Mixed Effect Models are Needed



What are mixed models?

- Extension of simple linear models
- Used when data is not independent
- Allows both fixed and random effects
 - Fixed effect: parameter that does not vary
 - Random effect: parameters that are themselves random variables
- Logistic mixed models: estimate odds that an event will occur in nested data

GLM and Mixed Effect Models

GLM

$$\text{Accuracy} \sim \boxed{\text{intercept} + \text{slope} * \text{fixed effect}} + \boxed{\text{error}}$$

systematic part random part

MM

$$\text{Accuracy} \sim \boxed{\text{intercept} + \text{slope} * \text{fixed effect}} + \boxed{\text{error}}$$

systematic part random effects residual error

Mixed Effect Models in R

*Dependent
variable: accuracy*

*Specifies that we'll give
a unique intercept to
each level of the
random effect*

*Nested random effects:
Video clips were clustered
within each actor.*

DV ~ clipcat*clipt*clipf + (1 + clipcat*clipt*clipf || actor)

*Independent
variables with a
3-way interaction*

*Specifies that we'll give a
unique slope to each level
of the random effect*

Modelling the data

	Fixed effects	Random effects	AIC
Model 1	clipcat * clipt * clipf	1 + clipcat * clipt * clipf subj	2888.9
Model 2	clipcat * clipt * clipf	1 + clipcat * clipt * clipf actor	2836.5
Model 3	clipcat * clipt * clipf	1 + clipcat * clipt * clipf clipn	2876

clipcat = category: food vs. music

clipt = statement truthfulness: true vs. false

clipf = preference: favorite vs. least favorite

Summary of the Model

Generalized linear mixed model fit by maximum likelihood (Laplace Approximation) ['glmerMod']

Family: binomial (logit)

Formula: `dv ~ clipcat * clipt * clipf + (1 + clipcat * clipt * clipf || actor)`

Data: DATA

AIC	BIC	logLik	deviance	df.resid
2836.516	3314.385	-1334.258	2668.516	2100

Fixed effects:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	0.10095	0.42231	0.239	0.8111
clipcat1	-0.16474	0.45507	-0.362	0.7173
clipt1	0.27447	0.49376	0.556	0.5783
clipf1	0.81266	0.43588	1.864	0.0623
clipcat1:clipt1	0.45974	0.70328	0.654	0.5133
clipcat1:clipf1	0.01306	0.56377	0.023	0.9815
clipt1:clipf1	-1.24970	0.71383	-1.751	0.0800
clipcat1:clipt1:clipf1	0.79154	0.79615	0.994	0.3201

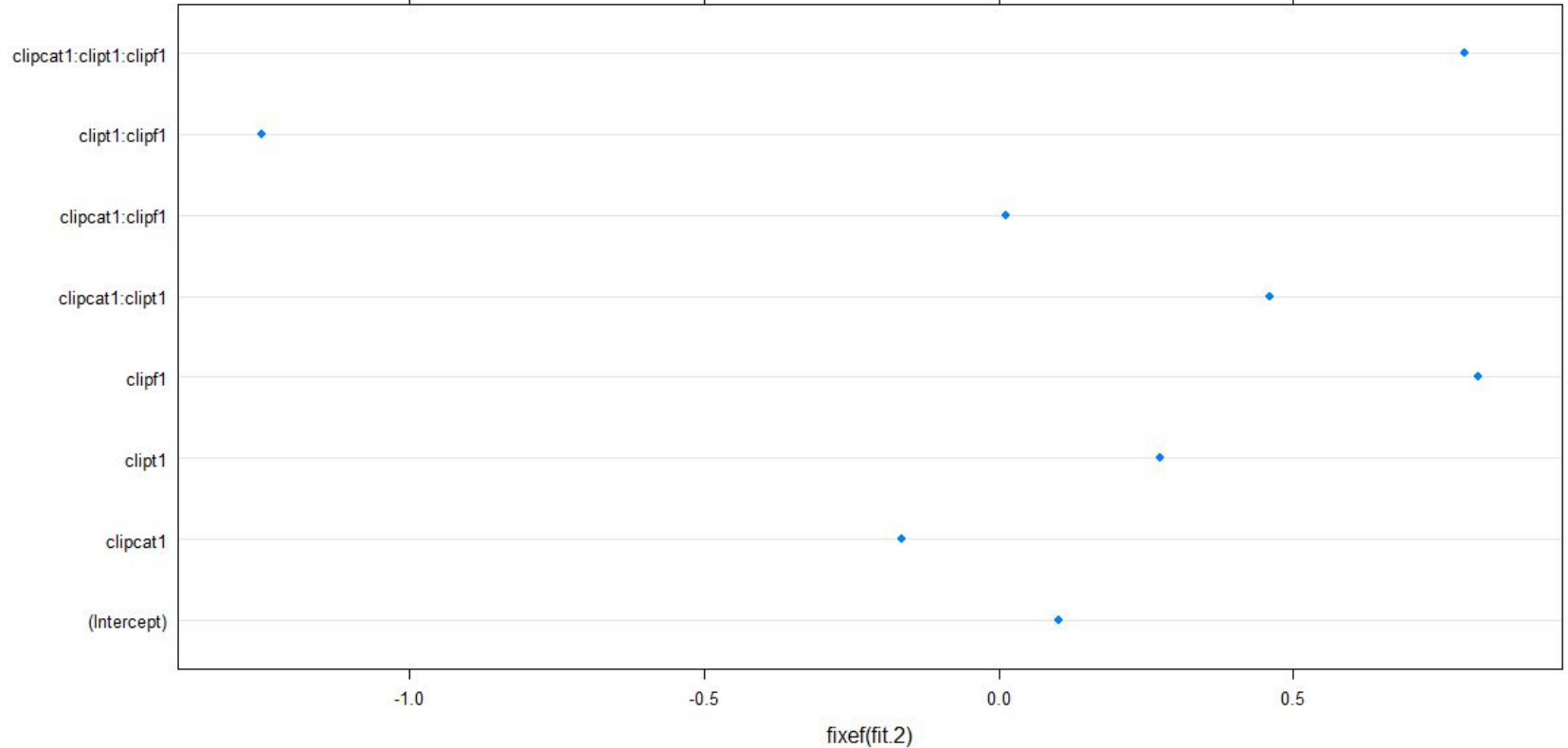
Random effects:

Groups	Name	Std.Dev.	Corr				
actor	(Intercept)	0.000e+00					
actor.1	clipcat0	1.022e-06					
	clipcat1	3.499e-06	-1.00				
actor.2	clipt0	0.000e+00					
	clipt1	2.780e-08					
actor.3	clipf0	2.468e-04					
	clipf1	4.648e-05	-1.00				
actor.4	clipcat0:clipt0	1.991e-01					
	clipcat1:clipt0	4.562e-02	1.00				
	clipcat0:clipt1	1.149e-01	-1.00	-1.00			
	clipcat1:clipt1	1.587e-01	-1.00	-1.00	1.00		
actor.5	clipcat0:clipf0	1.742e-01					
	clipcat1:clipf0	1.742e-02	-1.00				
	clipcat0:clipf1	4.922e-02	-1.00	1.00			
	clipcat1:clipf1	2.562e-03	-1.00	1.00	1.00		
actor.6	clipt0:clipf0	1.647e-01					
	clipt1:clipf0	2.213e-01	1.00				
	clipt0:clipf1	4.237e-02	-1.00	-1.00			
	clipt1:clipf1	2.730e-02	-1.00	-1.00	1.00		
actor.7	clipcat0:clipt0:clipf0	1.007e+00					
	clipcat1:clipt0:clipf0	7.881e-01	0.32				
	clipcat0:clipt1:clipf0	9.565e-01	0.31	0.41			
	clipcat1:clipt1:clipf0	4.429e-01	0.32	0.24	-0.66		
	clipcat0:clipt0:clipf1	7.238e-01	0.40	0.95	0.31	0.30	
	clipcat1:clipt0:clipf1	4.835e-01	0.40	0.73	0.59	-0.14	0.83
	clipcat0:clipt1:clipf1	7.459e-01	-0.68	-0.76	-0.62	-0.02	-0.85 -0.93
	clipcat1:clipt1:clipf1	4.471e-01	-0.08	-0.80	-0.49	0.01	-0.59 -0.31 0.39

Number of obs: 2184, groups: actor, 7

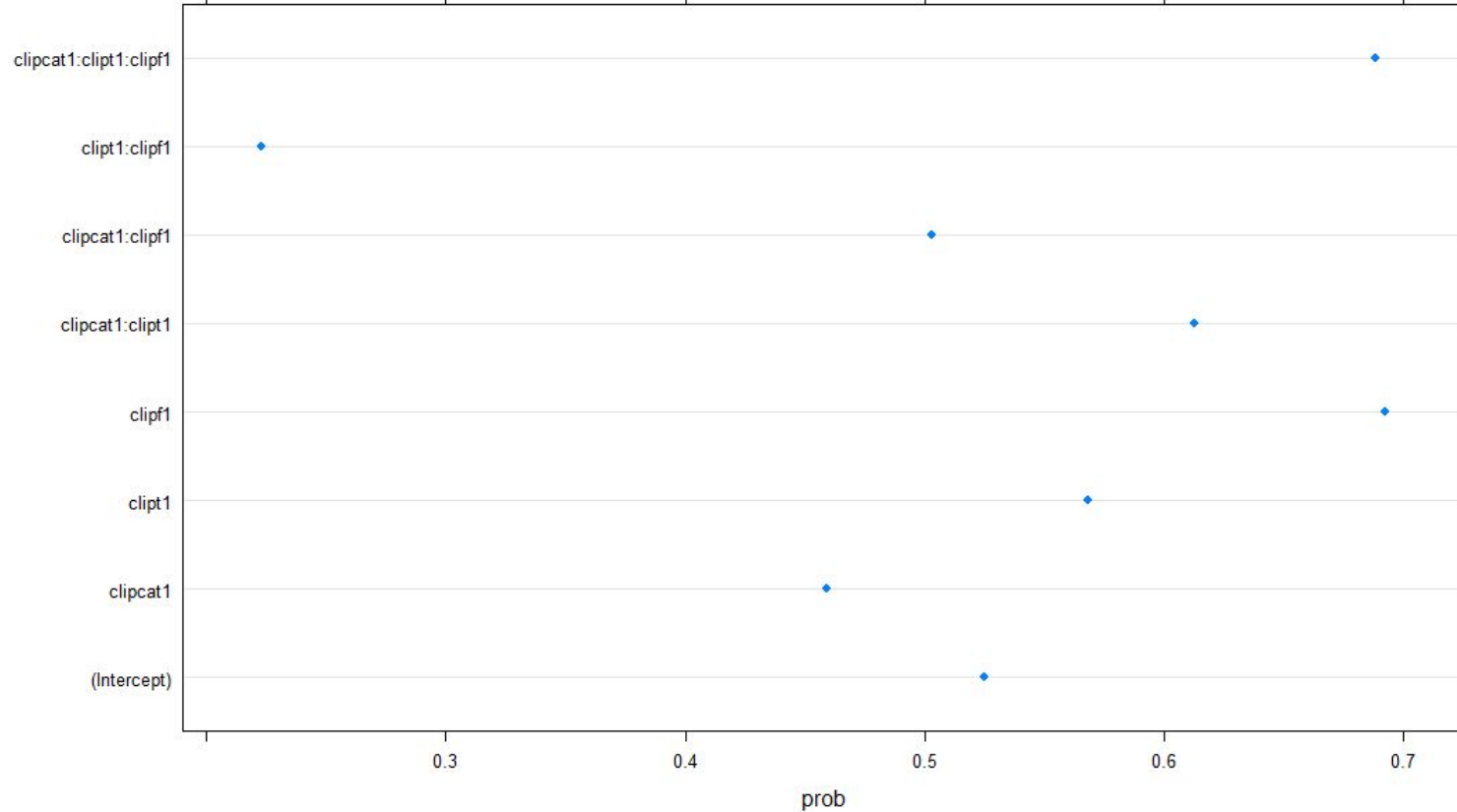
Results: Fixed Effects

$DV \sim \text{clipcat} * \text{clipt} * \text{clipf} + (1 + \text{clipcat} * \text{clipt} * \text{clipf} || \text{actor})$



Results: Fixed Effects

$DV \sim clipcat * clipt * clipf + (1 + clipcat * clipt * clipf | actor)$

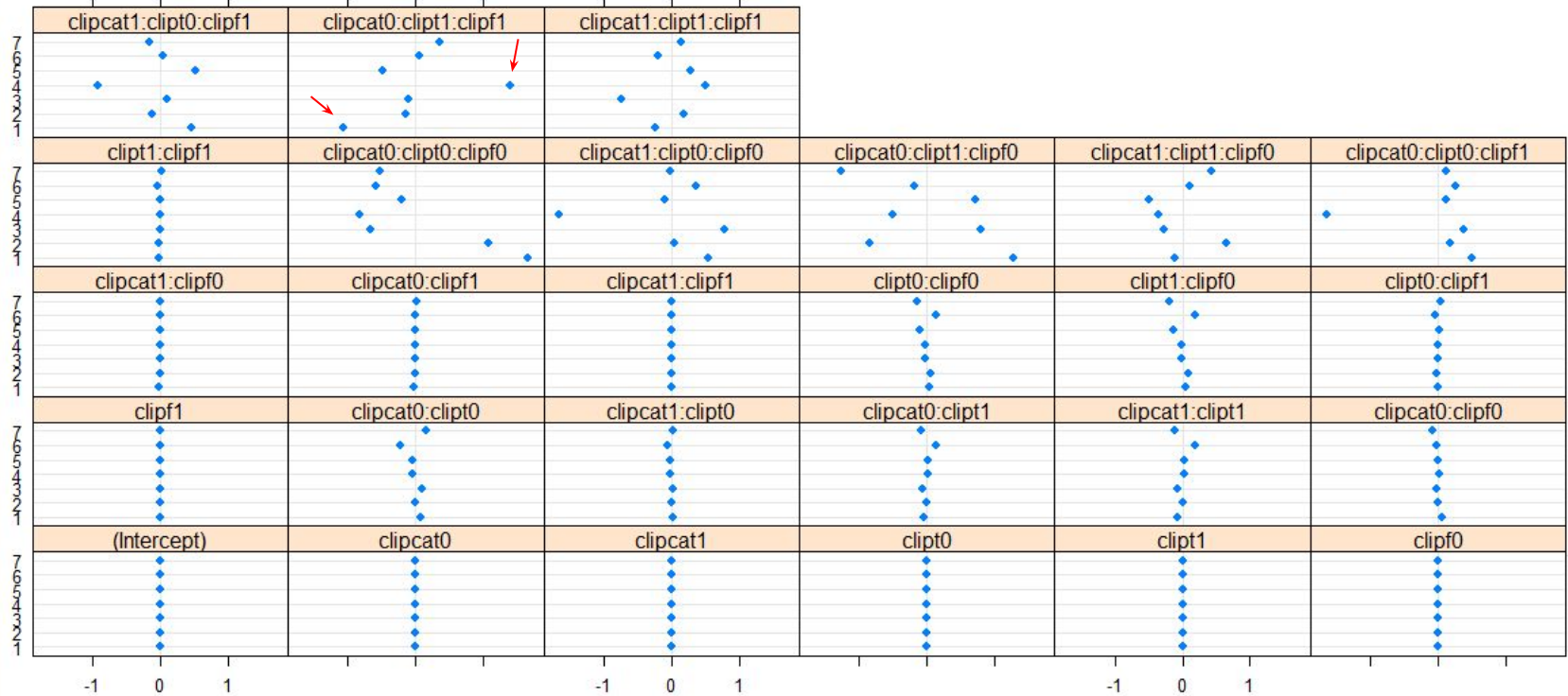


Fixed Effects

- Overall, participants perform at chance level
- Highest accuracy when actors were talking about their favorite category (clipf=1)
- Higher accuracy when actors were saying a truthful statement about their favorite category and when the category was food (Clipcat1:clipt1:clipf1)
- Lower accuracy when actors were saying something truthful about their favorite category (clipt1:clipf1) and both categories (food and music) are included
- No effect was statistically significant

Results: Random Effects

$$DV \sim \text{clipcat} * \text{clipt} * \text{clipf} + (1 + \text{clipcat} * \text{clipt} * \text{clipf} \mid \text{actor})$$



General Conclusion

The influence of clip properties depends on each other (interaction), and these interaction effects vary within actors

Discussion

- Individual differences in detecting lies?
Maybe not...
- Random effects within subjects didn't explain much more variance of accuracy compared with random effects within actors
- People who tell lies (actors) matter!

